

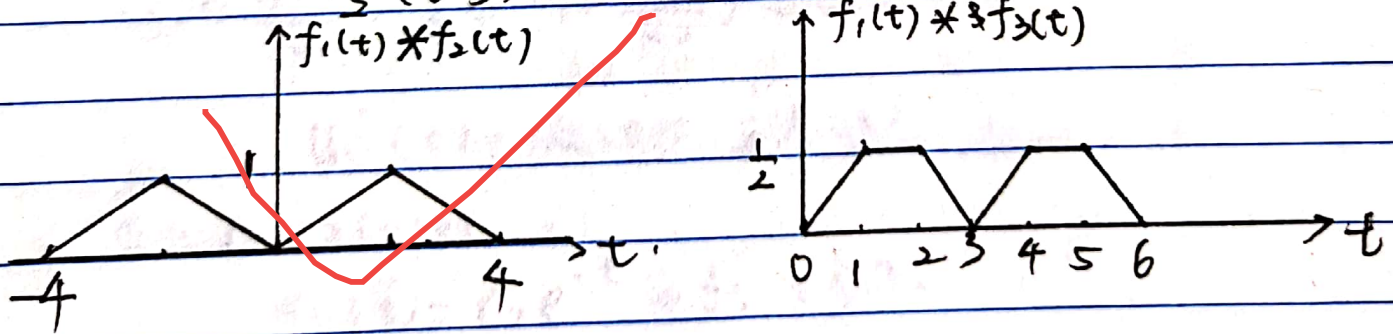
解: $f_1(t) = \frac{1}{2} [(t+2)\varepsilon(t+2) - 2t\varepsilon(t) + (t-2)\varepsilon(t-2)]$

$f_2(t) = \delta(t+2) + \delta(t-2)$

$f_4(t) = \delta(t-2) - \delta(t-3) + \delta(t-4)$

(1) $f_1(t) * f_2(t) = \int_{-\infty}^{\infty} f_1(\tau) \cdot f_2(t-\tau) d\tau$
 $= f_1(t+2) + f_1(t-2)$
 $= \frac{1}{2} (t+4)\varepsilon(t+4) - (t+2)\varepsilon(t+2) + t\varepsilon(t) - (t-2)\varepsilon(t-2)$
 $+ \frac{1}{2} (t-4)\varepsilon(t-4)$

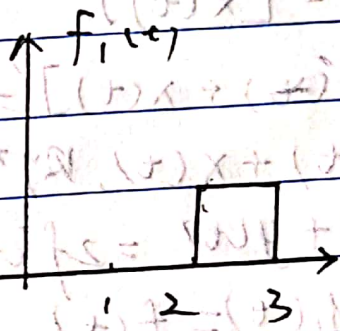
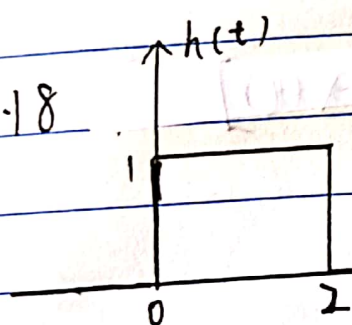
(3) $f_1(t) * f_3(t) = \int_{-\infty}^{\infty} f_1(\tau) \cdot f_3(t-\tau) d\tau = f_1(t-2) - f_1(t-3) * f_1(t-4)$
 $= \frac{1}{2} t\varepsilon(t) - \frac{1}{2} (t-1)\varepsilon(t-1) - \frac{1}{2} (t-2)\varepsilon(t-2) + (t-3)\varepsilon(t-3) - \frac{1}{2} (t-4)\varepsilon(t-4)$
 $- \frac{1}{2} (t-5)\varepsilon(t-5) + \frac{1}{2} (t-6)\varepsilon(t-6)$



2-17. (7) $f_1(t) = \varepsilon(t) - \varepsilon(t-4)$, $f_2(t) = \sin(\pi t) \varepsilon(t)$

$$\begin{aligned} f_1(t) * f_2(t) &= [\varepsilon(t) - \varepsilon(t-4)] * [\sin(\pi t) \varepsilon(t)] \\ &= [\varepsilon(t) \sin(\pi t) \varepsilon(t)] * [\delta(t) - \delta(t-4)] \\ &= \frac{1}{\pi} [1 - \cos(\pi t)] \varepsilon(t) * [\delta(t) - \delta(t-4)] \\ &= \frac{1}{\pi} [1 - \cos(\pi t)] [\varepsilon(t) - \varepsilon(t-4)] \end{aligned}$$

2-18



$h(t) = \varepsilon(t) - \varepsilon(t-2)$

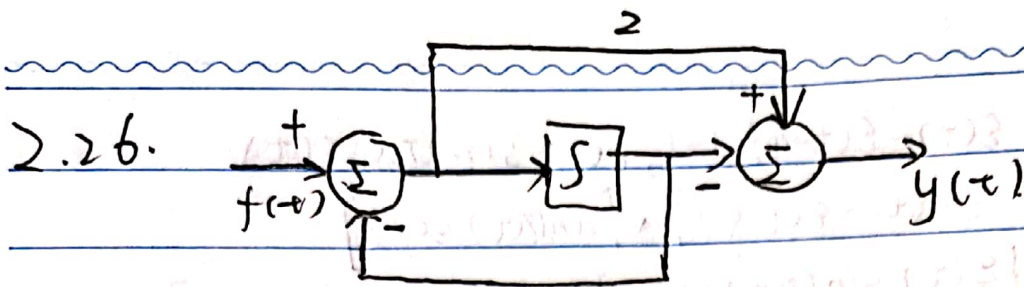
(1) $f(t) * \varepsilon(t)$

$$\begin{aligned} y_f &= f(t) * h(t) \\ &= \varepsilon(t) * \varepsilon(t) * [\delta(t) - \delta(t-2)] \\ &= t \varepsilon(t) * [\delta(t) - \delta(t-2)] \\ &= t \varepsilon(t) - (t-2) \varepsilon(t-2) \\ &= t [\varepsilon(t) - \varepsilon(t-2)] + 2 \varepsilon(t-2) \end{aligned}$$

(2) $f_1(t) = \varepsilon(t-2) - \varepsilon(t-3)$

$$\begin{aligned} y_{f_1} &= f_1(t) * h(t) \\ &= [\varepsilon(t-2) - \varepsilon(t-3)] * [\delta(t) - \delta(t-2)] \\ &= (t-2) \varepsilon(t-2) - (t-3) \varepsilon(t-3) - (t-4) \varepsilon(t-4) + (t-5) \varepsilon(t-5) \end{aligned}$$





解:

$$\begin{cases} x'(t) = f(t) - x(t) \\ y(t) = 2x'(t) - x(t) \end{cases}$$

$$y'(t) = 2[x'(t)]' - [x(t)]'$$

$$y(t) + y'(t) = 2[x'(t) + x(t)]' - [x'(t) + x(t)]$$

考虑式 $f(t) = x'(t) + x(t)$, 则有

$$y(t) + y'(t) = 2f'(t) - f(t)$$

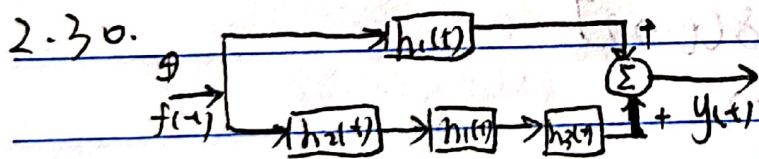
设 $y_1'(t) + y_1(t) = f(t)$

设其冲激响应为 $h_1(t)$. $h_1(0+) = 1$

$$h_1(t) = e^{-t} \varepsilon(t)$$

∴ 系统: $h(t) = 2h_1'(t) - h_1(t)$

$$h(t) = 2\delta(t) - 3e^{-t}\varepsilon(t)$$



令 $f(t) = \delta(t)$

$$h_1(t) = y_1(t) = f(t) * h_1(t) = \delta(t) * \varepsilon(t) = \varepsilon(t)$$

$$h_2(t) = y_2(t) = f(t) * h_2(t) * h_1(t) * h_3(t)$$

$$= \delta(t) * \delta(t-1) * \varepsilon(t) * [-\delta(t)]$$

$$= -\varepsilon(t-1)$$

$$h(t) = h_1(t) + h_2(t) = \varepsilon(t) - \varepsilon(t-1)$$

